

Round each part in the *answer* to the nearest tenth, unless otherwise indicated.

**Section 8.2 Formulas:**

1. A vector's components,  $\langle a, b \rangle$ , are defined by  $a = |\mathbf{V}| \cos \theta$  and  $b = |\mathbf{V}| \sin \theta$ .
2. A vector's **direction angle**,  $0^\circ \leq \theta < 360^\circ$ , is defined by first finding  $\hat{\theta}$ , using either  $\cos \hat{\theta} = \frac{|a|}{|\mathbf{V}|}$  or  $\sin \hat{\theta} = \frac{|b|}{|\mathbf{V}|}$ . To find  $\theta$ , either add or subtract  $\hat{\theta}$  with  $180^\circ$  or  $360^\circ$ , depending in which quadrant  $\mathbf{V}$  lies.
3. The angle measure,  $\alpha$ , between the two vectors,  $\mathbf{V}$  and  $\mathbf{W}$ :  $\cos \alpha = \frac{\mathbf{V} \cdot \mathbf{W}}{|\mathbf{V}| |\mathbf{W}|}$ ;  $0^\circ \leq \alpha \leq 180^\circ$ .

**Section 8.1:**

Given two vectors  $\mathbf{U} = \langle -12, -\frac{9}{4} \rangle$  and  $\mathbf{V} = \langle \frac{3}{5}, -6 \rangle$ , find the following

1.  $\mathbf{B} = 4\mathbf{U} - 10\mathbf{V}$
2.  $\mathbf{D} = \frac{8}{3}\mathbf{U} + \frac{10}{3}\mathbf{V}$

Given two vectors  $\mathbf{G} = -2\mathbf{i} + 6\mathbf{j}$  and  $\mathbf{H} = 3\mathbf{i} - 9\mathbf{j}$ , find the following. Write each answer in  $\mathbf{i}, \mathbf{j}$  form.

3.  $\mathbf{X} = \mathbf{G} - \mathbf{H}$
4.  $\mathbf{Z} = \frac{3}{2}\mathbf{G} + \frac{5}{3}\mathbf{H}$

**Section 8.2:**

Given the magnitude and direction angle of a vector, find its components.

5.  $|\mathbf{K}| = 40$  and  $\theta = 78.5^\circ$
6.  $|\mathbf{L}| = 8$  and  $\theta = 164^\circ$
7.  $|\mathbf{M}| = 15$  and  $\theta = 199^\circ$
8.  $|\mathbf{N}| = 56$  and  $\theta = 333^\circ$

Find the **direction angle**,  $\theta$ , of the given vector. Round  $\theta$  to the nearest tenth of a degree.

9.  $\mathbf{A} = \langle 9, 2 \rangle$
10.  $\mathbf{B} = \langle -6, 7 \rangle$
11.  $\mathbf{C} = \langle -3, -2 \rangle$
12.  $\mathbf{D} = \langle 6, -11 \rangle$

Given two vectors, find the angle,  $\alpha$ , between them. Round  $\alpha$  to the nearest whole number.\*

**13.**  $\mathbf{V} = \langle -4, 15 \rangle$  and  $\mathbf{W} = \langle 9, -5 \rangle$

**14.**  $\mathbf{S} = \langle 2, 9 \rangle$  and  $\mathbf{T} = \langle 3, 1 \rangle$

**15.**  $\mathbf{X} = \langle -8, 6 \rangle$  and  $\mathbf{Y} = \langle -9, -12 \rangle$

**16.**  $\mathbf{P} = \langle 6, -10 \rangle$  and  $\mathbf{Q} = \langle -9, 15 \rangle$

\*For #13-16, use this following outline:

- i) Find both  $|\mathbf{V}|$  and  $|\mathbf{W}|$
- ii) Find the dot product  $\mathbf{V} \cdot \mathbf{W}$
- iii) Find  $\alpha$  using the  $\cos\alpha$  formula, above.