## Rationalize all denominators, as necessary.

1. What degree measure represents the given portion of a circle? Draw a central angle that has that same number of degrees.
seven-ninths of a circle

2. In $\triangle A B C, m \angle B=22^{\circ} 18^{\prime} 41^{\prime \prime}$. Find $m \angle A$.

3. $\angle A B C$ and $\angle X Y Z$ are supplementary angles. Given the measure of $\angle A B C$, find $m \angle X Y Z$.

$$
m \angle A B C=102^{\circ} 28^{\prime} 15^{\prime \prime}
$$

4. $\triangle X Y Z$ is an isosceles triangle. $\angle X$ and $\angle Y$ are the congruent base angles. Given $m \angle Z$, find $m \angle X$. (Write the answer in DMS.)

$$
m \angle Z=86^{\circ} 47^{\prime}
$$

5. At right, $\overline{T M}$ bisects $\angle P T R$.
a) If $m \angle P T M=28^{\circ} 43^{\prime} 52^{\prime \prime}$, find $m \angle P T R$.
b) If $m \angle P T R=63^{\circ} 31^{\prime} 18^{\prime \prime}$, find $m \angle P T M$.

6. Consider a circle centered at the origin that passes through $(-4,2 \sqrt{5})$.
Note: $2 \sqrt{5} \approx 4.5$
a) Find the radius of the circle
b) Draw its graph.
c) What is the equation of the circle?
7. Verify that the given point is on the unit circle.
$\left(-\frac{5 \sqrt{3}}{9}, \frac{\sqrt{6}}{9}\right)$
8. Use the identity $\sin \theta= \pm \sqrt{1-\cos ^{2} \theta}$ to find $\sin \theta$.
$\cos \theta=-\frac{\sqrt{5}}{3}$ and $\theta$ terminates in QIII.
9. The radius of a circle is 4 inches, and the measure of $\operatorname{Arc}_{\mathrm{AB}}$ is $\frac{20 \pi}{3}$. Determine the measure of the central angle that subtends Arcab.
10. The radius of a circle is 6 inches, and the measure of a central angle, $\boldsymbol{m} \angle \mathrm{AOB}$ is $80^{\circ}$. Determine the length of the arc it subtends.

Find the value of $x$ in the given triangle and simplify completely.
11.

12.


Find the values of $h, m, p, x$, and $y$, which represent the lengths of the sides of these triangles. Simplify completely.

a) $x=4$
b) $h=9$
c) $m=12$
14.

a) $y=5$
b) $x=6 \sqrt{3}$
c) $h=9 \sqrt{2}$
15. Based on the given information, in which quadrant does $\theta$ terminate.
a) $\sec \theta<0$ and $\sin \theta>0$
b) $\tan \theta>0$ and $\cos \theta<0$
c) $\csc \theta>0$ and $\tan \theta>0$
d) $\tan \theta<0$ and $\sin \theta<0$
e) $\cos \theta<0$ and $\cot \theta>0$
f) $\csc \theta>0$ and $\sec \theta>0$
g) $\sin \theta<0$ and $\sec \theta>0$
h) $\cot \theta<0$ and $\cos \theta<0$

For each given angle measure, (i) locate it in a circle using standard position, and (ii) identify an angle that is coterminal with it and ...
16. between $0^{\circ}$ and $360^{\circ}$
$\theta=-240^{\circ}$

17. between $0^{\circ}$ and $-360^{\circ}$

$$
\theta=980^{\circ}
$$



Locate the given point in the $x$ - $y$-plane, and draw a positive angle $\theta$ whose terminal side contains the point. Then, find the values of the six trig functions of $\theta$ and simplify.


Find and simplify the requested trig values based on the information given. Rationalize the denominator, if necessary.
20. If $\theta$ terminates in Quadrant IV
and $\cot \theta=-\frac{3}{4}$, find
$\sin \theta=$
$\tan \theta=$
$\sec \theta=$
21. If $\theta$ terminates in Quadrant II
and $\csc \theta=\frac{3}{\sqrt{5}}$, find
$\sin \theta=$
$\cos \theta=$
$\tan \theta=$
22. Use the given triangles and mark them however you wish to assist you in finding the following trig values. (Simplify and rationalize the denominator, if necessary.)


| $\sin 30^{\circ}=$ | $\sin 60^{\circ}=$ | $\sin 45^{\circ}=$ |
| :--- | :--- | :--- |
| $\cos 30^{\circ}=$ | $\cos 60^{\circ}=$ | $\cos 45^{\circ}=$ |
| $\tan 30^{\circ}=$ | $\tan 60^{\circ}=$ | $\tan 45^{\circ}=$ |
| $\cot 30^{\circ}=$ | $\cot 60^{\circ}=$ | $\cot 45^{\circ}=$ |
| $\sec 30^{\circ}=$ | $\sec 60^{\circ}=$ | $\sec 45^{\circ}=$ |
| $\csc 30^{\circ}=$ | $\csc 60^{\circ}=$ | $\csc 45^{\circ}=$ |

Evaluate each. Simplify; rationalize the denominator, if necessary.
23. $2 \sqrt{3} \sin 60^{\circ}$
24. $\sqrt{\cot 45^{\circ}}$
25. $\sqrt{\sec 60^{\circ}}$
26. $\left(\tan 30^{\circ}\right)^{2}$
27. $\left(\csc 45^{\circ}\right)^{2}$
28. $\tan 60^{\circ} \cdot \cos 30^{\circ}$

Write each in terms of sine and cosine only, and simplify completely.
29. $\sin \theta \cdot \cot \theta+\sec \theta$
30. $\sec \theta-\tan \theta \cdot \sin \theta$

