Name

Rationalize all denominators, as necessary.

1. What degree measure represents the given portion of a circle? Draw a central angle that has that same number of degrees.

seven-ninths of a circle



b)

2. $\angle ABC$ and $\angle XYZ$ are supplementary angles. Given the measure of $\angle ABC$, find $m\angle XYZ$.

 $m \angle ABC = 102^{\circ} 28' 15''$

3. In $\triangle ABC$, $m \angle B = 22^{\circ} 18'41''$. Find $m \angle A$.

R

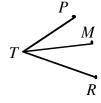
4. $\triangle XYZ$ is an isosceles triangle. $\angle X$ and $\angle Y$ are the congruent base angles. Given $m \angle Z$, find $m \angle X$. (Write the answer in DMS.)

 $m \angle Z = 86^{\circ} 47'$

5. At right, \overline{TM} bisects $\angle PTR$.

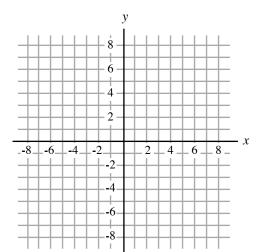
a) If $m \angle PTM = 28^{\circ} 43'52''$, find $m \angle PTR$.

If $m \angle PTR = 63^{\circ} 31'18''$, find $m \angle PTM$.



6. Consider a circle centered at the origin that passes through (-4, $2\sqrt{5}$). Note: $2\sqrt{5} \approx 4.5$

a) Find the radius of the circle



- b) Draw its graph.
- c) What is the equation of the circle?
- 7. Verify that the given point is on the unit circle.

 $\left(-\frac{5\sqrt{3}}{9}, \frac{\sqrt{6}}{9}\right)$

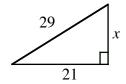
8. Use the identity $\sin \theta = \pm \sqrt{1 - \cos^2 \theta}$ to find $\sin \theta$.

 $\cos\theta = -\frac{\sqrt{5}}{3}$ and θ terminates in QIII.

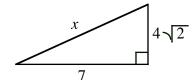
- 9. The radius of a circle is 4 inches, and the measure of Arc_{AB} is $\frac{20\pi}{3}$. Determine the measure of the central angle that subtends Arc_{AB} .
- 10. The radius of a circle is 6 inches, and the measure of a central angle, m ∠AOB is 80°. Determine the length of the arc it subtends.

Find the value of x in the given triangle and simplify completely.

11.

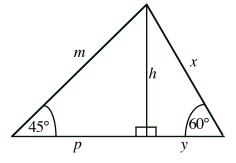


12.

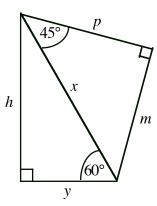


Find the values of h, m, p, x, and y, which represent the lengths of the sides of these triangles. Simplify completely.

13.



14.



a)
$$x = 4$$

a)
$$y = 5$$

b)
$$h = 9$$

b)
$$x = 6\sqrt{3}$$

c)
$$m = 12$$

c)
$$h = 9\sqrt{2}$$

15. Based on the given information, in which quadrant does θ terminate.

a)
$$\sec \theta < 0$$
 and $\sin \theta > 0$

b)
$$\tan \theta > 0$$
 and $\cos \theta < 0$

c)
$$\csc\theta > 0$$
 and $\tan\theta > 0$

d)
$$\tan \theta < 0$$
 and $\sin \theta < 0$

e)
$$\cos\theta < 0$$
 and $\cot\theta > 0$

f)
$$\csc \theta > 0$$
 and $\sec \theta > 0$

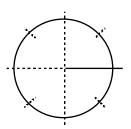
g)
$$\sin \theta < 0$$
 and $\sec \theta > 0$

h)
$$\cot \theta < 0$$
 and $\cos \theta < 0$

For each given angle measure, (i) locate it in a circle using standard position, and (ii) identify an angle that is coterminal with it and ...

16. between 0° and 360°

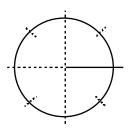




What is r?

17. between
$$0^{\circ}$$
 and -360°

$$\theta = 980^{\circ}$$



What is r?

Locate the given point in the x-y-plane, and draw a positive angle θ whose terminal side contains the point. Then, find the values of the six trig functions of θ and simplify.

18.
$$(3, -\sqrt{7})$$

$$\sin\theta =$$

$$\cos\theta =$$

$$\tan\theta =$$

$$\cot \theta =$$

$$sec\theta =$$

$$csc\theta =$$

$$\sin\theta =$$

$$\cos\theta =$$

$$\tan\theta =$$

$$\tan \theta =$$

$$\cot \theta =$$

$$sec\theta =$$

$$\csc\theta =$$

Find and simplify the requested trig values based on the information given. Rationalize the denominator, if necessary.

20. If
$$\theta$$
 terminates in Quadrant IV

and
$$\cot \theta = -\frac{3}{4}$$
, find

$$\sin\theta =$$

$$\tan\theta =$$

$$sec\theta =$$

21. If
$$\theta$$
 terminates in Quadrant II

and
$$\csc\theta = \frac{3}{\sqrt{5}}$$
, find

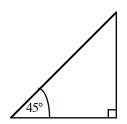
$$\sin\theta =$$

$$\cos\theta =$$

$$\tan\theta =$$

22. Use the given triangles and mark them however you wish to assist you in finding the following trig values. (Simplify and rationalize the denominator, if necessary.)





$$\sin 30^{\circ} =$$

$$\sin 45^{\circ} =$$

$$\cos 30^{\circ} =$$

$$\cos 60^{\circ} =$$

$$\cos 45^{\circ} =$$

$$\tan 30^{\circ} =$$

$$\tan 45^{\circ} =$$

$$\cot 45^{\circ} =$$

$$sec 30^{\circ} =$$

$$sec 60^{\circ} =$$

$$sec 45^{\circ} =$$

$$csc 30^{\circ} =$$

$$csc 60^{\circ} =$$

$$csc 45^{\circ} =$$

Evaluate each. Simplify; rationalize the denominator, if necessary.

23.
$$2\sqrt{3} \sin 60^{\circ}$$

$$24. \quad \sqrt{\cot 45^{\circ}}$$

25.
$$\sqrt{\sec 60^\circ}$$

26.
$$(\tan 30^\circ)^2$$

27.
$$(\csc 45^{\circ})^2$$

28.
$$\tan 60^{\circ} \cdot \cos 30^{\circ}$$

Write each in terms of sine and cosine only, and simplify completely.

29.
$$\sin\theta \cdot \cot\theta + \sec\theta$$

30.
$$\sec \theta - \tan \theta \cdot \sin \theta$$