

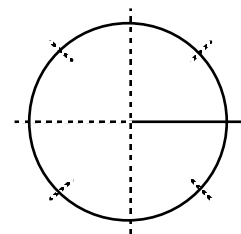
**Rationalize all denominators, as necessary.**

Rationalize the denominator and simplify the expression.

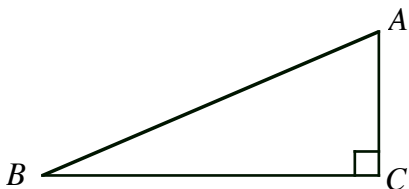
1.  $\frac{-6}{3 - \sqrt{6}}$

What degree measure represents the given portion of a circle? Draw a central angle that has that same number of degrees.

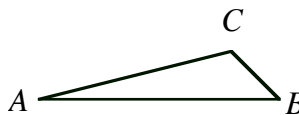
2.  $\frac{7}{9}$  of a circle



3. In  $\triangle ABC$ ,  $m\angle B = 22^\circ 18' 41''$ . Find  $m\angle A$ .



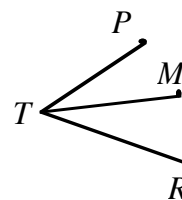
4. In  $\triangle ABC$ ,  $m\angle A = 17^\circ 26' 38''$  and  $m\angle B = 44^\circ 31' 55''$ . Find  $m\angle C$ .



5. At right,  $\overline{TM}$  bisects  $\angle PTR$ .

a) If  $m\angle PTM = 28^\circ 43' 52''$ , find  $m\angle PTR$ .

b) If  $m\angle PTR = 63^\circ 31' 18''$ , find  $m\angle PTM$ .

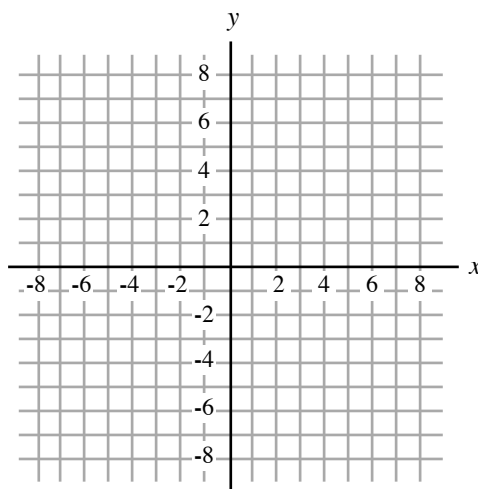


6. Consider a circle centered at the origin that passes through  $(-4, 2\sqrt{5})$ .

a) Find the radius of the circle

b) Draw its graph.

c) What is the equation of the circle?



Verify that the given point is on the unit circle.

7.  $\left(-\frac{5\sqrt{3}}{9}, \frac{\sqrt{6}}{9}\right)$

Use the identity  $\sin\theta = \pm\sqrt{1 - \cos^2\theta}$  to find  $\sin\theta$ .

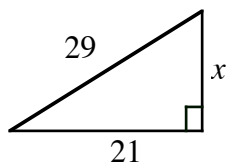
8.  $\cos\theta = -\frac{\sqrt{5}}{3}$  and  $\theta$  terminates in QIII..

9. The radius of a circle is 4 inches, and the measure of  $\text{Arc}_{AB}$  is  $\frac{20\pi}{3}$ . Determine the measure of the central angle that subtends  $\text{Arc}_{AB}$ .

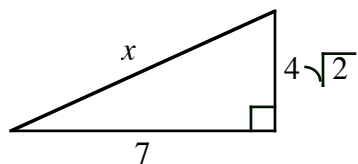
10. The radius of a circle is 6 inches, and the measure of a central angle,  $m\angle AOB$  is  $80^\circ$ . Determine the length of the arc it subtends.

Find the value of  $x$  in the given triangle and simplify completely.

11.

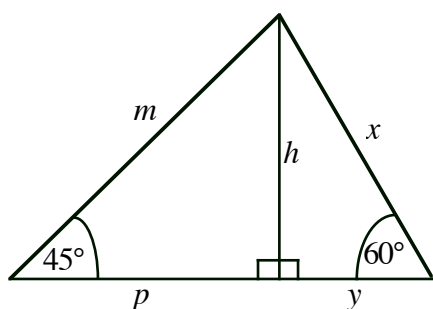


12.



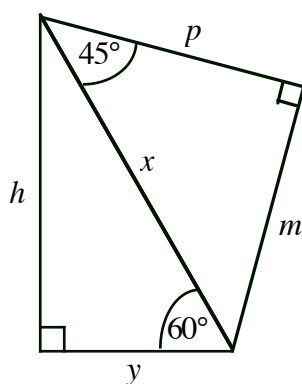
Find the values of  $h$ ,  $m$ ,  $p$ ,  $x$ , and  $y$ , which represent the lengths of the sides of these triangles. Simplify completely.

13.



- a)  $x = 4$        $y =$   
                           $h =$   
                           $p =$   
                           $m =$
- b)  $h = 9$        $y =$   
                           $x =$   
                           $p =$   
                           $m =$
- c)  $m = 12$        $p =$   
                           $m =$   
                           $y =$   
                           $x =$

14.



- a)  $y = 5$        $h =$   
                           $x =$   
                           $m =$   
                           $p =$
- b)  $x = 6\sqrt{3}$        $y =$   
                           $h =$   
                           $m =$   
                           $p =$
- c)  $h = 9\sqrt{2}$        $y =$   
                           $x =$   
                           $m =$   
                           $p =$

**15.** Based on the given information, in which quadrant does  $\theta$  terminate?

**a)**  $\sec\theta < 0$  and  $\sin\theta > 0$

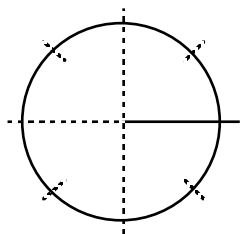
**b)**  $\tan\theta > 0$  and  $\cos\theta < 0$

**c)**  $\csc\theta > 0$  and  $\tan\theta > 0$

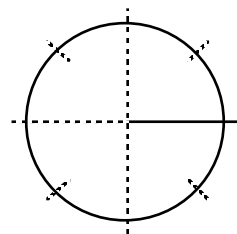
**d)**  $\cot\theta < 0$  and  $\cos\theta < 0$

For each given angle measure, (i) locate it in a circle using standard position, and (ii) identify an angle **between  $0^\circ$  and  $360^\circ$**  that is coterminal with it.

**16.**  $\theta = -240^\circ$



**17.**  $\theta = 930^\circ$



Locate the given point in the  $x$ - $y$ -plane, and draw a positive angle  $\theta$  whose terminal side contains the point. Then, find the values of the six trig functions of  $\theta$  and simplify.

**18.**  $(3, -\sqrt{7})$

$\sin\theta =$

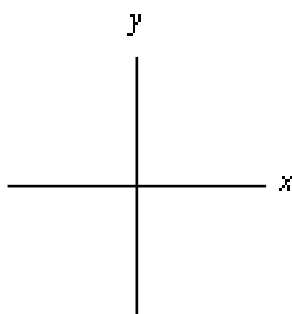
$\cos\theta =$

$\tan\theta =$

$\cot\theta =$

$\sec\theta =$

$\csc\theta =$



What is  $r$ ?

**19.**  $(0, 2)$

$\sin\theta =$

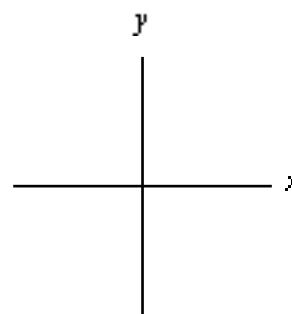
$\cos\theta =$

$\tan\theta =$

$\cot\theta =$

$\sec\theta =$

$\csc\theta =$



What is  $r$ ?

Find and simplify the requested trig values based on the information given. Rationalize the denominator, if necessary.

**20.** If  $\theta$  terminates in Quadrant IV

and  $\cot \theta = -\frac{3}{4}$ , find

$$\sin \theta =$$

$$\tan \theta =$$

$$\sec \theta =$$

**21.** If  $\theta$  terminates in Quadrant II

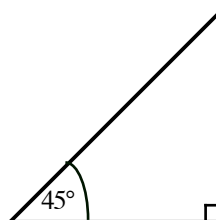
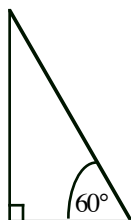
and  $\csc \theta = \frac{3}{\sqrt{5}}$ , find

$$\sin \theta =$$

$$\cos \theta =$$

$$\tan \theta =$$

**22.** Use the given triangles and mark them however you wish to assist you in finding the following trig values. (Simplify and rationalize the denominator, if necessary.)



$$\sin 30^\circ =$$

$$\sin 60^\circ =$$

$$\sin 45^\circ =$$

$$\cos 30^\circ =$$

$$\cos 60^\circ =$$

$$\cos 45^\circ =$$

$$\tan 30^\circ =$$

$$\tan 60^\circ =$$

$$\tan 45^\circ =$$

$$\cot 30^\circ =$$

$$\cot 60^\circ =$$

$$\cot 45^\circ =$$

$$\sec 30^\circ =$$

$$\sec 60^\circ =$$

$$\sec 45^\circ =$$

$$\csc 30^\circ =$$

$$\csc 60^\circ =$$

$$\csc 45^\circ =$$

Evaluate each. Simplify; rationalize the denominator, if necessary.

23.  $2\sqrt{3} \sin 60^\circ$

24.  $\sqrt{\cot 45^\circ}$

25.  $\sqrt{\sec 60^\circ}$

26.  $(\tan 30^\circ)^2$

27.  $(\csc 45^\circ)^2$

28.  $\tan 60^\circ \cdot \cos 30^\circ$

Write each in terms of sine and cosine only, and then simplify completely.

29.  $\sin \theta \cdot \cot \theta + \cos \theta$

30.  $\sec \theta - \tan \theta \cdot \sin \theta$

Demonstrate that the equation is an identity by transforming the left side (only) to be equivalent to the right side.

31.  $\frac{\tan \theta}{\sin \theta \cos \theta} = \sec^2 \theta$

32.  $\csc \theta \tan \theta - \cos \theta = \frac{\sin^2 \theta}{\cos \theta}$