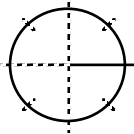


**Rationalize all denominators, as necessary.**

1. What degree measure represents the given portion of a circle? Draw a central angle that has that same number of degrees.

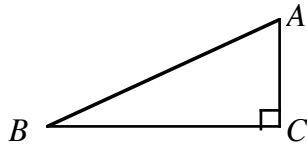
seven-ninths of a circle



2.  $\angle ABC$  and  $\angle XYZ$  are supplementary angles. Given the measure of  $\angle ABC$ , find  $m\angle XYZ$ .

$$m\angle ABC = 102^\circ 28' 15''$$

3. In  $\triangle ABC$ ,  $m\angle B = 22^\circ 18' 41''$ . Find  $m\angle A$ .

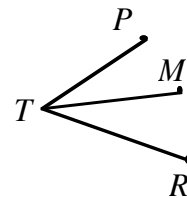


4.  $\triangle XYZ$  is an isosceles triangle.  $\angle X$  and  $\angle Y$  are the congruent base angles. Given  $m\angle Z$ , find  $m\angle X$ . (Write the answer in DMS.)

$$m\angle Z = 86^\circ 47'$$

5. At right,  $\overline{TM}$  bisects  $\angle PTR$ .

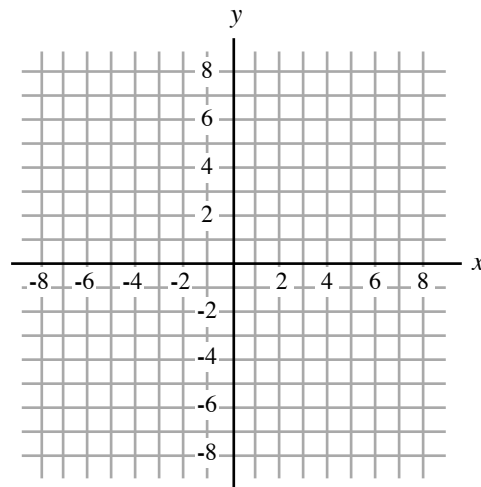
- a) If  $m\angle PTM = 28^\circ 43' 52''$ , find  $m\angle PTR$ .  
 b) If  $m\angle PTR = 63^\circ 31' 18''$ , find  $m\angle PTM$ .



6. Consider a circle centered at the origin that passes through  $(-4, 2\sqrt{5})$ .

Note:  $2\sqrt{5} \approx 4.5$

- a) Find the radius of the circle  
 b) Draw its graph.  
 c) What is the equation of the circle?



7. Verify that the given point is on the unit circle.

$$\left(-\frac{5\sqrt{3}}{9}, \frac{\sqrt{6}}{9}\right)$$

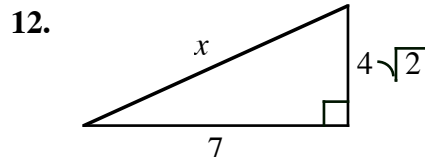
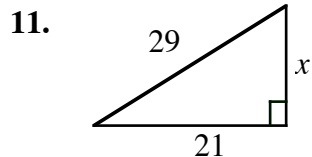
8. Use the identity  $\sin\theta = \pm\sqrt{1 - \cos^2\theta}$  to find  $\sin\theta$ .

$$\cos\theta = -\frac{\sqrt{5}}{3} \text{ and } \theta \text{ terminates in QIII.}$$

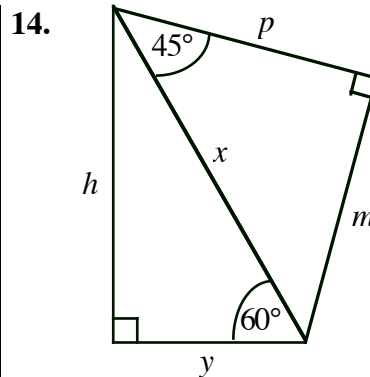
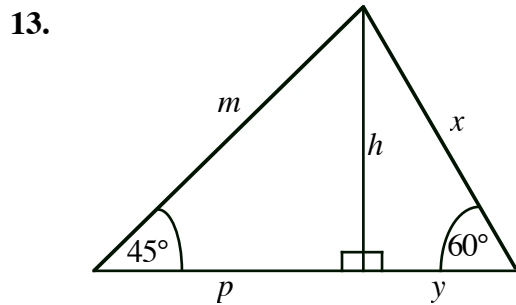
9. The radius of a circle is 4 inches, and the measure of  $\text{Arc}_{AB}$  is  $\frac{20\pi}{3}$ . Determine the measure of the central angle that subtends  $\text{Arc}_{AB}$ .

10. The radius of a circle is 6 inches, and the measure of a central angle,  $m\angle AOB$  is  $80^\circ$ . Determine the length of the arc it subtends.

Find the value of  $x$  in the given triangle and simplify completely.



Find the values of  $h$ ,  $m$ ,  $p$ ,  $x$ , and  $y$ , which represent the lengths of the sides of these triangles. Simplify completely.



- a)  $x = 4$   
 b)  $h = 9$   
 c)  $m = 12$

- a)  $y = 5$   
 b)  $x = 6\sqrt{3}$   
 c)  $h = 9\sqrt{2}$

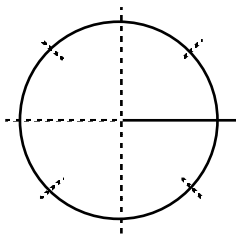
15. Based on the given information, in which quadrant does  $\theta$  terminate.

- a)  $\sec\theta < 0$  and  $\sin\theta > 0$       b)  $\tan\theta > 0$  and  $\cos\theta < 0$   
 c)  $\csc\theta > 0$  and  $\tan\theta > 0$       d)  $\tan\theta < 0$  and  $\sin\theta < 0$   
 e)  $\cos\theta < 0$  and  $\cot\theta > 0$       f)  $\csc\theta > 0$  and  $\sec\theta > 0$   
 g)  $\sin\theta < 0$  and  $\sec\theta > 0$       h)  $\cot\theta < 0$  and  $\cos\theta < 0$

For each given angle measure, (i) locate it in a circle using standard position, and (ii) identify an angle that is coterminal with it and ...

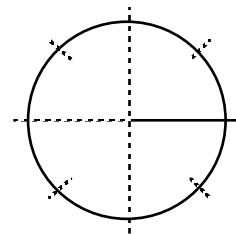
**16.** between  $0^\circ$  and  $360^\circ$

$$\theta = -240^\circ$$



**17.** between  $0^\circ$  and  $-360^\circ$

$$\theta = 980^\circ$$



Locate the given point in the  $x$ - $y$ -plane, and draw a positive angle  $\theta$  whose terminal side contains the point. Then, find the values of the six trig functions of  $\theta$  and simplify.

**18.**  $(3, -\sqrt{7})$

$$\sin \theta =$$

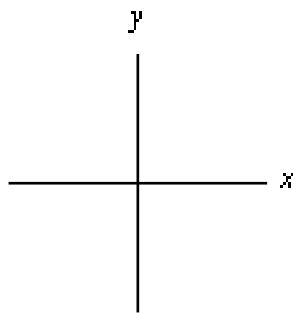
$$\cos \theta =$$

$$\tan \theta =$$

$$\cot \theta =$$

$$\sec \theta =$$

$$\csc \theta =$$



What is  $r$ ?

**19.**  $(0, 2)$

$$\sin \theta =$$

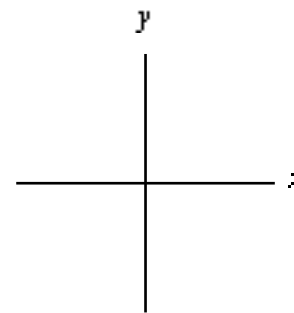
$$\cos \theta =$$

$$\tan \theta =$$

$$\cot \theta =$$

$$\sec \theta =$$

$$\csc \theta =$$



What is  $r$ ?

Find and simplify the requested trig values based on the information given. Rationalize the denominator, if necessary.

**20.** If  $\theta$  terminates in Quadrant IV

$$\text{and } \cot \theta = -\frac{3}{4}, \text{ find}$$

$$\sin \theta =$$

$$\tan \theta =$$

$$\sec \theta =$$

**21.** If  $\theta$  terminates in Quadrant II

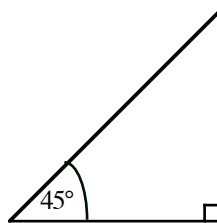
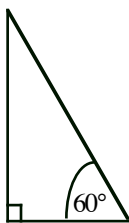
$$\text{and } \csc \theta = \frac{3}{\sqrt{5}}, \text{ find}$$

$$\sin \theta =$$

$$\cos \theta =$$

$$\tan \theta =$$

22. Use the given triangles and mark them however you wish to assist you in finding the following trig values. (Simplify and rationalize the denominator, if necessary.)



$$\sin 30^\circ =$$

$$\sin 60^\circ =$$

$$\sin 45^\circ =$$

$$\cos 30^\circ =$$

$$\cos 60^\circ =$$

$$\cos 45^\circ =$$

$$\tan 30^\circ =$$

$$\tan 60^\circ =$$

$$\tan 45^\circ =$$

$$\cot 30^\circ =$$

$$\cot 60^\circ =$$

$$\cot 45^\circ =$$

$$\sec 30^\circ =$$

$$\sec 60^\circ =$$

$$\sec 45^\circ =$$

$$\csc 30^\circ =$$

$$\csc 60^\circ =$$

$$\csc 45^\circ =$$

Evaluate each. Simplify; rationalize the denominator, if necessary.

23.  $2\sqrt{3} \sin 60^\circ$

24.  $\sqrt{\cot 45^\circ}$

25.  $\sqrt{\sec 60^\circ}$

26.  $(\tan 30^\circ)^2$

27.  $(\csc 45^\circ)^2$

28.  $\tan 60^\circ \cdot \cos 30^\circ$

Write each in terms of sine and cosine only, and simplify completely.

29.  $\sin \theta \cdot \cot \theta + \sec \theta$

30.  $\sec \theta - \tan \theta \cdot \sin \theta$

Demonstrate that the equation is an identity by transforming the left side (only) to be equivalent to the right side.

31.  $\frac{\tan \theta}{\sin \theta \cos \theta} = \sec^2 \theta$

32.  $\csc \theta \tan \theta - \cos \theta = \frac{\sin^2 \theta}{\cos \theta}$